Field-Controlled Phase Separation at the Impurity-Induced Magnetic Ordering in the Spin-Peierls Magnet CuGeO$_3$

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The paramagnetic fraction surviving at the impurity-induced antiferromagnetic phase transition in the spin-Peierls magnet CuGeO$_3$ is found to increase with an external magnetic field. This effect is explained by the competition of the Zeeman interaction and of the exchange interaction of local antiferromagnetic clusters formed on the spin-gap background near impurities.

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Inhomogeneity has become a fundamental concept in physics and chemistry and plays an important role in various classes of materials ranging from relaxor ferroelectrics to superconducting cuprates. In strongly correlated electron systems, the physics of the inhomogeneous state is relevant to the formation of stripe phases in high-$T_c$ cuprates [1] and charge-ordered manganites [2,3], as well as to disorder driven metal-to-insulator transitions accompanied by colossal magnetoresistance effects in manganese perovskites [4] and Eu-based hexaborides [5]. Here we add another chapter to this fundamental approach: The occurrence of a field-controlled inhomogeneous state in spin-Peierls magnets.

Spin-chain magnets of spin-Peierls [6] or Haldane [7] type reveal a quantum-disordered singlet ground state which is separated from the excited magnetic states by an energy gap. Consequently, the disordered ground state is stable against the influence of the crystal field or a weak interchain exchange. Nevertheless, these quantum para-magnets may be driven into the ordered state by means of weak doping, both magnetic and nonmagnetic [8,9]. Impurity-induced magnetic ordering is explained by the local destruction of the singlet state and a concomitant onset of local staggered magnetization. This local antiferromagnetic (AFM) order consists of approximately ten correlated spins of a chain with a total magnetic moment of $\mu_B$ [10,11]. It has been argued that the resonating-valence-bond character of the spin correlations at low distances is responsible for the robust local staggered magnetization [12]. According to these models, the staggered magnetization attains a maximum value at the sites of a spin chain near the impurity and decays exponentially with the distance from the impurity. Such areas of the staggered magnetization of about ten interspin distances in size were detected experimentally in a doped spin-Peierls magnet [13]. The overlap of the wings of these ordered areas and a weak interchain exchange should result in long-range AFM order [10,14,15].

In spin-Peierls systems the spin-gap originates from the magnetoelastic instability of a 3D crystal containing spin $S = 1/2$ chains. At the spin-Peierls instability, $T_{SP}$, the chains become dimerized with the exchange-integral taking in turn two values $J + \delta$ and $J - \delta$. The dimerization produces a gain in exchange energy which exceeds the loss in elastic energy [16]. The spin-Peierls transition and the impurity-induced ordering were studied in detail in CuGeO$_3$ with $T_{SP} = 14.5$ K [17]. Doping prevents dimerization, i.e., the temperature $T_{SP}$ of a doped crystal is lower than that of a pure one, and at an impurity concentration $x$ exceeding a threshold value $x_c$, the lattice remains uniform.

Thus, depending on the concentration, the Néel transition occurs on the dimerized (i.e., spin-gap) or uniform (gapless) background. The ($T$, $x$) diagram is reported in a variety of papers, for the case of nonmagnetic Mg doping, with a detailed map of lattice and magnetic states given in Ref. [18].

Because the staggered magnetization induced by an impurity is localized on a short distance, the ordered phase should be highly inhomogeneous. It was found experimentally [17,19,20] that below the Néel temperature $T_N$ the AFM and paramagnetic (PM) resonance signals coexist. Considering the spatial inhomogeneity, it means that the order parameter varies in space from a maximum value till zero, and consequently a real microscopic phase separation into AFM and PM phases occurs. These experiments demonstrated the coexistence of PM and AFM responses in a magnetic field near $H = 12$ kOe. For nonzero temperature, AFM areas of different sizes embedded in the spin-gap matrix are expected [17]. Accordingly, macroscopic AFM regions provide AFM resonance and susceptibility. Small AFM clusters, i.e., isolated chain fragments, provide PM resonance signals and a Curie-like susceptibility. The nu-
Numerical simulation [21] confirmed a strongly inhomogeneous ground state with practically 100% spatial modulation of the order parameter, implying a phase separation at a finite temperature. Thus, impurity-induced ordering on a spin-gap background provides a new kind of microscopic phase separation. As outlined above, phase separation is intensively studied, and the electronic phase separation into ferromagnetic droplets and antiferromagnetic regions in manganites (see, e.g., [4]) and the stripe formation of electron density in high-temperature superconductors [1] are paramount examples. These examples come along with the presence of charge carriers or with a redistribution of their density. But the phase separation in a doped spin-gap magnet takes place on a perfect dielectric background. Here the phase separation results from the interplay of the basic singlet background and nanoscopic AFM areas restored at impurity sites. In this Letter we show that this new kind of microscopic phase separation can be controlled by an external magnetic field, and this field effect is documented below.

The motivation to explore the influence of a magnetic field on the impurity-induced order arises from the hypothesis that the correlation of the local order parameters of neighboring small AFM areas should be broken by the magnetic field, if a parallel orientation of the net magnetic moments hampers the coherent AFM order in these two areas (see Fig. 1). Indeed, such an influence of the magnetic field on the impurity-ordered phase can be deduced from our magnetic resonance experiment, which quantitatively probes the ratio of PM and AFM fractions dependent on the field.

We used the same set of Cu$_{1-x}$Mg$_x$GeO$_3$ single crystals as for the investigations of phase diagram [18] and phase separation [17]. Electron spin resonance (ESR) enables the detection of two phases, because AFM and paramagnetic phases have different resonance frequencies (or different resonance fields, when measured at a fixed frequency $\nu$) [17]. The low-temperature ESR signal arises predominantly from the impurities, because the susceptibility of the spin-Peierls background is frozen due to the spin gap. The characteristic feature of the AFM-resonance mode is the nonzero frequency in zero field. The PM resonance of $S = 1/2$ centers follows the simple frequency-field relation $h \nu = g \mu_B H$, and its integral intensity is proportional to the static susceptibility, hence, to the number of free spins. The fraction of the sample, which remains paramagnetic below the Néel point, can be derived as the ratio of the integral intensities of the PM resonance signals below and above $T_N$. We have performed the measurements of this ratio in different magnetic fields by taking the ESR absorption as a function of the magnetic field at different microwave frequencies. By means of a set of transmission-type ESR spectrometers covering the range from 18 to 40 GHz and using additionally a commercial Bruker ELEXSYS X-Band spectrometer (9.5 GHz), we recorded the ESR lines in the field range $3 \leq H \leq 12$ kOe.

As a typical example, Fig. 2 shows the evolution of the ESR line shape with temperature in Cu$_{1-x}$Mg$_x$GeO$_3$ ($x = 1.71\%$) obtained at a microwave frequency $\nu = 36.2$ GHz. Above the Néel temperature $T_N = 2.25$ K the absorption...
spectrum is well described by a single-Lorentzian line. Additional absorption arises at lower fields, when the temperature decreases below the Néel point. The resonance field of this additional signal decreases with decreasing temperature. At \( \nu > 18 \) GHz it is observable in the whole temperature range and its intensity grows on cooling. Concomitantly, the intensity of the PM absorption decreases. Thus, at low temperatures and at \( \nu > 18 \) GHz the ESR absorption is dominated by the component with the temperature-dependent resonance field. The frequency-field dependence of this mode reveals the characteristics of an orthorhombic AFM and can be identified as AFM resonance \([17]\). The Néel temperature \( T_N \) can be determined as the temperature of the onset of the AFM-resonance absorption. The values of \( T_N \) obtained for all samples in this way are in agreement with the results of magnetization studies \([18]\). The X-band measurements (inset of Fig. 2) reveal two coexisting lines only in a narrow temperature interval below \( T_N \), with only the PM component visible at low temperatures. The AFM component disappears closely below \( T_N \) because the AFM-resonance gap becomes larger than the microwave frequency. Nevertheless, the diminishing PM component indicates the coexistence of the increasing AFM fraction. Note that for a normal AFM transition only an AFM absorption signal should be present below \( T_N \). For \( \text{Cu}_{x-0.04}\text{Mg}_x\text{GeO}_3 \) we observe this normal scenario at \( x > 0.04 \), where the dimerization is fully suppressed. At low microwave frequencies, in contrast to the situation demonstrated in the inset of Fig. 2, the ESR line in a normal AFM disappears immediately below \( T_N \).

The ESR lines taken at different temperatures and frequencies were fitted by a sum of two Lorentzians, providing a direct measure of the intensity of AFM (dashed line) and paramagnetic resonances (dotted line in Fig. 2). The temperature dependences of the integrated intensities of the paramagnetic component are shown in Fig. 3 for three different microwave frequencies. Extrapolating the temperature dependence of the intensity of the PM component to the transition point allows the determination of the fraction of the sample remaining paramagnetic at the Néel temperature. An unequivocal determination of the two ESR components at temperatures just below \( T_N \) is rather uncertain and an error of about 20% of the total intensity occurs close to the transition temperature for \( \nu = 26.4 \) and 36.0 GHz. At 9.5 GHz, this error is about 10%. However, the observed increase of the paramagnetic fraction with increasing microwave frequency is significantly beyond this error, as shown in Fig. 3. For \( x = 1.71\% \) the PM fraction increases as a function of frequency (i.e., field) from 0.2 at 9.5 GHz to 0.8 at 36 GHz. This field dependence of the paramagnetic fraction at the temperature just below \( T_N \) is given in Fig. 4 for two concentrations. The relative intensity of the PM component at the Néel point increases with increasing magnetic field for both samples.

Concentration dependences of the PM fraction are shown in the inset of Fig. 4. The data taken at different frequencies are normalized to the microwave frequency (i.e., to the ESR field in the PM phase). The normalized dependences demonstrate a qualitatively similar behavior with the PM fraction vanishing at \( x \approx 0.04 \). The concentration dependence of the PM fraction can be understood in terms of the model developed previously \([17]\): with increasing impurity concentration the volume of the PM phase decreases, because the distances between impurities decrease and the regions of local AFM order more and more overlap. Hence, the volume fraction remaining for the undisturbed singlet matrix and for isolated AFM chain fragments decreases. Besides that, at \( x > 3.5\% \) the dimerization is suppressed and neither a spin gap nor phase separation exists.

The field dependence of the PM fraction can be explained using the concepts of Refs. \([10,14,15]\). The local order parameter decays exponentially with the distance from the impurity, measured along the chain. At nonzero temperature the AFM correlation of spin projections will be lost at a distance \( L \) from the impurity atom, and this distance may be estimated by the relation

\[
JS^2 \exp \left(-\frac{2L}{\xi}\right) \sim k_B T.
\]  

Here \( J \) denotes the exchange-integral value and \( \xi \) characterizes the magnetic correlation length in the corresponding direction. The ensemble of correlated spins in the chain fragment of length \( L \) near the impurity and of the spins from the neighboring chains, correlated with the spins in the fragment due to the interchain exchange, are denoted as
“cluster,” each cluster with a net magnetic moment of $\mu_B$. As temperature decreases, the size $L$ increases and the clusters begin to overlap; thus the area of coherent AFM order increases. In a magnetic field the Zeeman energy of the clusters attains a minimum, if the net magnetic moments of all clusters are aligned parallel to the field, but the exchange energy reaches a minimum at a coherent correlation of local AFM order parameters. Thus, an external magnetic field destroys the AFM correlation of neighboring clusters positioned as shown in Fig. 1. The correlation of the order parameters of two clusters on a chain fragment containing an odd number of spins will be destroyed by a magnetic field given approximately by the relation

$$g\mu_B H \sim JS^2 \exp\left[-\frac{2L}{\xi}\right].$$

(2)

Therefore, the magnetic field enhances the number of clusters with uncorrelated AFM order parameters and results in an increase of the PM fraction of the sample. In other words, the increase of the field should increase the PM fraction below the transition point, in accordance with the experimental observations. This simplified consideration does not include the interchain correlation which may also be influenced by the magnetic field. In this way, a strong magnetic field destroys the long-range AFM order, but the local order near the impurities will survive. Therefore, this scenario can also explain the anomalously strong field dependence of the Néel temperature reported recently for the impurity-induced ordering in the Haldane magnet PbNi$_2$V$_2$O$_8$ [22].

In conclusion, the observation of a paramagnetic ESR signal below the impurity-induced Néel transition reveals a new type of AFM order, with a field-dependent microscopic separation of magnetic phases. The fraction of the paramagnetic phase is enlarged by application of an external magnetic field. Within a qualitative model, considering the competition between exchange interaction and Zeeman energy of the local antiferromagnetic clusters formed around the impurities, the influence of the magnetic field on the phase separation is explained. This behavior should be relevant for the large class of spin-gap magnets.

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